

Lecture Plan

Name of the College: Government College of Arts, Science and Commerce, Sanquelim-Goa

Name of Faculty: Ms. Raksha. R. Sankatala

Subject: Mathematics

Paper code: MAT-524

Program: M.Sc.

Division: -

Academic year: 2024-25

Semester: I

Total Lectures: 60

Course Objectives: This course develops the ability to solve partial differential equations of first and second order by standard methods.

Expected Course Outcome:

- 1) Solve partial differential equations of first and second order.
- 2) Model initial and boundary value problems.
- 3) Analyse the properties of solution.
- 4) Interpret solutions in a physical context.
- 5) Understand analogies between mathematical descriptions of different (wave) phenomena in physics and engineering.

Student Learning Outcome:

Student will be able to

- 1) Distinguish between types of partial differential equations.
- 2) Solve problems of linear and nonlinear partial differential equations.
- 3) Solve problems of heat and wave equation.

| Month | Lecture From | Lecture To | No. of lectures allotted | Topic, Subtopic to be covered | Exercise/ Assignment | ICT Tools | Reference books |
|-------------|--------------|------------|--------------------------|--|--------------------------------|--------------------------|---|
| | 08/07/2024 | 13/07/2024 | 4 | Simultaneous differential equations of the first and first degree in three variables: Methods of solutions of $\frac{dx}{P} = \frac{dy}{Q} = \frac{dz}{R}$. Pfaffian differential forms and equations. | Exercises on the topic covered | Smart Board, Chalk Board | T. Amarnath, An elementary course in Partial Differential Equations |
| | 15/07/2024 | 20/07/2024 | 4 | Solutions of Pfaffian differential equations in three variables. | Exercises on the topic covered | Smart Board, Chalk Board | T. Amarnath, An elementary course in Partial Differential Equations |
| | 22/07/2024 | 27/07/2024 | 4 | First order PDE's: Origin and classification. Solutions of linear and Nonlinear First order PDE's. | Exercises on the topic covered | Smart Board, Chalk Board | T. Amarnath, An elementary course in Partial Differential Equations |
| July August | 29/07/2024 | 03/08/2024 | 4 | Methods of characteristics. Charpit's Methods. | Exercises on the topic covered | Smart Board, Chalk Board | T. Amarnath, An elementary course in Partial Differential Equations |
| August | 05/08/2024 | 10/08/2024 | 4 | Jacobi's method. | Exercises on the topic covered | Smart Board, Chalk Board | T. Amarnath, An elementary course in Partial Differential Equations |
| | 12/08/2024 | 17/08/2024 | 4 | Second Order Linear Partial Differential Equations: Origin. Linear equations with constant coefficients in | Exercises on the topic covered | Smart Board, Chalk Board | T. Amarnath, An elementary course in |

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| | | | two independent variables. Linear equations with variable coefficients. | | | Partial Differential Equations |
| | 19/08/2024 | 24/08/2024 | 4 | Classification. Reduction to canonical form. (only for the case of two independent variables). | Exercises on the topic covered | Smart Board, Chalk Board T. Amarnath, An elementary course in Partial Differential Equations |
| | 26/08/2024 | 31/08/2024 | 4 | Methods of solving PDE: Method of separation of variables. Use of integral transforms. (Laplace and Fourier). | Exercises on the topic covered | Smart Board, Chalk Board T. Amarnath, An elementary course in Partial Differential Equations |
| September | 02/09/2024 | 07/09/2024 | 4 | Wave Equation: One dimensional Wave equation. D'Alembert solution, Wave equation -Infinite string case. | Exercises on the topic covered | Smart Board, Chalk Board T. Amarnath, An elementary course in Partial Differential Equations |
| | 16/09/2024 | 21/09/2024 | 4 | Laplace Equation: Harmonic function. Basic properties of harmonic functions. | Exercises on the topic covered | Smart Board, Chalk Board T. Amarnath, An elementary course in Partial Differential Equations |
| | 23/09/2024 | 28/09/2024 | 4 | Laplace Equation: Laplace equation. Translational and rotational invariance of Laplace equations. | Exercises on the topic covered | Smart Board, Chalk Board T. Amarnath, An elementary course in Partial Differential Equations |
| September October | 30/09/2024 | 05/10/2024 | 4 | Boundary value problems. Uniqueness of solutions of Dirichlet and Neumann problems. | Exercises on the topic covered | Smart Board, Chalk Board T. Amarnath, An elementary course in Partial Differential Equations |

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| October | 07/10/2024 | 12/10/2024 | 4 | Mean value theorem for harmonic functions. Maximum and minimum principle for harmonic functions. | Exercises on the topic covered | Smart Board, Chalk Board | T. Amarnath, An elementary course in Partial Differential Equations |
| | 14/10/2024 | 19/10/2024 | 4 | Uniqueness and stability for Dirichlet problem | Exercises on the topic covered | Smart Board, Chalk Board | T. Amarnath, An elementary course in Partial Differential Equations |
| | 21/10/2024 | 23/10/2024 | 4 | Heat Equation: Infinite rod case. Non homogeneous equation. | Exercises on the topic covered | Smart Board, Chalk Board | T. Amarnath, An elementary course in Partial Differential Equations |

*** Assessment Rubrics**

| Component | Max Marks |
|-------------------|-----------|
| ISA 1 | 20 |
| ISA 2 | 20 |
| ISA 3 | 20 |
| Semester End Exam | 40 |